

Chapter 468

Equivalence Tests for the Ratio of Two Negative Binomial Rates

Introduction

This procedure may be used to calculate power and sample size for equivalence tests involving the ratio of two Negative Binomial rates.

The calculation details upon which this procedure is based are found in Zhu (2016). Some of the details are summarized below.

Technical Details

Definition of Terms

The following table presents the various terms that are used.

Group	1 (Control)	2 (Treatment)
Sample size	N_1	N_2
Individual event rates	λ_1	λ_2

Dispersion parameter: φ (Negative Binomial dispersion)

Average exposure time: μ_t

Equivalence ratios: R_{Lower} ($R_{Lower} < 1$); R_{Upper} ($R_{Upper} > 1$)

Sample size ratio: $\theta = N_2/N_1$

Equivalence Tests for the Ratio of Two Negative Binomial Rates

Hypotheses

The equivalence test hypotheses are

$$H_0: \frac{\lambda_2}{\lambda_1} \leq R_{Lower} \text{ or } \frac{\lambda_2}{\lambda_1} \geq R_{Upper} \quad \text{vs.} \quad H_1: R_{Lower} < \frac{\lambda_2}{\lambda_1} < R_{Upper}$$

where $R_{Lower} < 1$ and $R_{Upper} > 1$.

For a given equivalence test with significance level α , a two-sided confidence interval with $100(1 - 2\alpha)\%$ confidence is typically used. H_0 is rejected if the confidence interval falls completely between R_{Lower} and R_{Upper} .

Power Calculation

Power Calculation

Zhu (2016) bases the power calculation on an equivalence test derived from a Negative Binomial regression model. The power calculation is

$$Power = \Phi\left(\frac{\sqrt{N_1}(\log(\lambda_2/\lambda_1) - \log R_{Lower}) - z_{\alpha}\sqrt{V_0^-}}{\sqrt{V_1}}\right) + \Phi\left(\frac{\sqrt{N_1}(\log R_{Upper} - \log(\lambda_2/\lambda_1)) - z_{\alpha}\sqrt{V_0^+}}{\sqrt{V_1}}\right) - 1$$

where

$$V_1 = \frac{1}{\mu_t} \left(\frac{1}{\lambda_1} + \frac{1}{\theta\lambda_2} \right) + \frac{(1 + \theta)\varphi}{\theta}$$

and V_0^- and V_0^+ may be calculated in any of 3 ways.

V_0 Calculation Method 1 (using assumed true rates)

$$V_{01}^- = V_{01}^+ = \frac{1}{\mu_t} \left(\frac{1}{\lambda_1} + \frac{1}{\theta\lambda_2} \right) + \frac{(1 + \theta)\varphi}{\theta}$$

Using Method 1, V_0^- , V_0^+ , and V_1 are equal.

V_0 Calculation Method 2 (fixed marginal total)

$$V_{02}^- = \frac{(1 + R_{Lower}\theta)^2}{\mu_t R_{Lower}\theta(\lambda_1 + \theta\lambda_2)} + \frac{(1 + \theta)\varphi}{\theta}$$

$$V_{02}^+ = \frac{(1 + R_{Upper}\theta)^2}{\mu_t R_{Upper}\theta(\lambda_1 + \theta\lambda_2)} + \frac{(1 + \theta)\varphi}{\theta}$$

V_0 Calculation Method 3 (restricted maximum likelihood estimation)

$$V_{03}^- = \frac{2a}{\mu_t(-b - \sqrt{b^2 - 4ac})} \left(1 + \frac{1}{\theta R_{Lower}} \right) + \frac{(1 + \theta)\varphi}{\theta}$$

where

$$a = -\varphi\mu_t R_{Lower}(1 + \theta),$$

$$b = \varphi\mu_t(\lambda_1 R_{Lower} + \theta\lambda_2) - (1 + \theta R_{Lower}),$$

$$c = \lambda_1 + \theta\lambda_2$$

V_{03}^+ is calculated in the same way, replacing R_{Lower} with R_{Upper} .

Equivalence Tests for the Ratio of Two Negative Binomial Rates

Zhu (2016) did not give a recommendation regarding whether Method 1, 2, or 3 should be used, except to say that “in summary, based on scenarios simulated, all of the sample size methods derived in this paper calculated reasonably accurate sample sizes for the intended power. Although some methods seemed slightly better than the others for some scenarios, the sample size differences were very small relative to the actual sample sizes.”

Procedure Options

This section describes the options that are specific to this procedure. These are located on the Design tab. For more information about the options of other tabs, go to the Procedure Window chapter.

Design Tab

The Design tab contains the parameters associated with this test such as the Negative Binomial rates, sample sizes, alpha, and power.

Solve For

Solve For

This option specifies the parameter to be solved for from the other parameters.

Variance Calculation

Variance Calculation Method

Select among the three methods for calculating the V_0 variance component (see the documentation above for details).

- **Using Assumed True Rates**
For this choice, the variance component V_0 is based the values entered for λ_1 and λ_2 .
- **Fixed Marginal Total**
This method assumes a fixed number of events.
- **Restricted Maximum Likelihood Estimation**
This method uses the variance calculation based on restricted maximum likelihood estimation.

Power and Alpha

Power

This option specifies one or more values for power. Power is the probability of rejecting a false null hypothesis, and is equal to one minus Beta. Beta is the probability of a type-II error, which occurs when a false null hypothesis is not rejected. In this procedure, a type-II error occurs when you fail to reject the null hypothesis of inferiority when in fact the treatment mean is non-inferior.

Values must be between zero and one. Historically, the value of 0.80 (Beta = 0.20) was used for power. Now, 0.90 (Beta = 0.10) is also commonly used.

A single value may be entered here or a range of values such as *0.8 to 0.95 by 0.05* may be entered.

Alpha

This option specifies one or more values for the probability of a type-I error. A type-I error occurs when a true null hypothesis is rejected. In this procedure, a type-I error occurs when rejecting the null hypothesis of inferiority when in fact the treatment group is not inferior to the reference group.

Equivalence Tests for the Ratio of Two Negative Binomial Rates

Values must be between zero and one. Historically, the value of 0.05 has been used for alpha. This means that about one test in twenty will falsely reject the null hypothesis. You should pick a value for alpha that represents the risk of a type-I error you are willing to take in your experimental situation.

You may enter a range of values such as *0.01 0.05 0.10* or *0.01 to 0.10 by 0.01*.

$\mu(t)$ (Average Exposure Time)

$\mu(t)$ (Average Exposure Time)

Enter a value (or range of values) for the average exposure (observation) time for each subject in each group. A value of one is commonly entered when exposure times are all equal. The range is $\mu(t) > 0$. You can enter a single value such as 1 or a series of values such as *0.8 0.9 1* or *0.8 to 1.2 by 0.1*.

Sample Size (When Solving for Sample Size)

Group Allocation

Select the option that describes the constraints on $N1$ or $N2$ or both.

The options are

- Equal ($N1 = N2$)**
 This selection is used when you wish to have equal sample sizes in each group. Since you are solving for both sample sizes at once, no additional sample size parameters need to be entered.
- Enter $N2$, solve for $N1$**
 Select this option when you wish to fix $N2$ at some value (or values), and then solve only for $N1$. Please note that for some values of $N2$, there may not be a value of $N1$ that is large enough to obtain the desired power.
- Enter $R = N2/N1$, solve for $N1$ and $N2$**
 For this choice, you set a value for the ratio of $N2$ to $N1$, and then PASS determines the needed $N1$ and $N2$, with this ratio, to obtain the desired power. An equivalent representation of the ratio, R , is

$$N2 = R * N1.$$
- Enter percentage in Group 1, solve for $N1$ and $N2$**
 For this choice, you set a value for the percentage of the total sample size that is in Group 1, and then PASS determines the needed $N1$ and $N2$ with this percentage to obtain the desired power.

$N2$ (Sample Size, Group 2)

This option is displayed if Group Allocation = "Enter $N2$, solve for $N1$ "

$N2$ is the number of items or individuals sampled from the Group 2 population.

$N2$ must be ≥ 2 . You can enter a single value or a series of values.

R (Group Sample Size Ratio)

This option is displayed only if Group Allocation = "Enter $R = N2/N1$, solve for $N1$ and $N2$."

R is the ratio of $N2$ to $N1$. That is,

$$R = N2 / N1.$$

Use this value to fix the ratio of $N2$ to $N1$ while solving for $N1$ and $N2$. Only sample size combinations with this ratio are considered.

Equivalence Tests for the Ratio of Two Negative Binomial Rates

$N2$ is related to $N1$ by the formula:

$$N2 = [R \times N1],$$

where the value $[Y]$ is the next integer $\geq Y$.

For example, setting $R = 2.0$ results in a Group 2 sample size that is double the sample size in Group 1 (e.g., $N1 = 10$ and $N2 = 20$, or $N1 = 50$ and $N2 = 100$).

R must be greater than 0. If $R < 1$, then $N2$ will be less than $N1$; if $R > 1$, then $N2$ will be greater than $N1$. You can enter a single or a series of values.

Percent in Group 1

This option is displayed only if Group Allocation = "Enter percentage in Group 1, solve for N1 and N2."

Use this value to fix the percentage of the total sample size allocated to Group 1 while solving for $N1$ and $N2$. Only sample size combinations with this Group 1 percentage are considered. Small variations from the specified percentage may occur due to the discrete nature of sample sizes.

The Percent in Group 1 must be greater than 0 and less than 100. You can enter a single or a series of values.

Sample Size (When Not Solving for Sample Size)

Group Allocation

Select the option that describes how individuals in the study will be allocated to Group 1 and to Group 2.

The options are

- **Equal ($N1 = N2$)**
This selection is used when you wish to have equal sample sizes in each group. A single per group sample size will be entered.
- **Enter $N1$ and $N2$ individually**
This choice permits you to enter different values for $N1$ and $N2$.
- **Enter $N1$ and R , where $N2 = R * N1$**
Choose this option to specify a value (or values) for $N1$, and obtain $N2$ as a ratio (multiple) of $N1$.
- **Enter total sample size and percentage in Group 1**
Choose this option to specify a value (or values) for the total sample size (N), obtain $N1$ as a percentage of N , and then $N2$ as $N - N1$.

Sample Size Per Group

This option is displayed only if Group Allocation = "Equal ($N1 = N2$)."

The Sample Size Per Group is the number of items or individuals sampled from each of the Group 1 and Group 2 populations. Since the sample sizes are the same in each group, this value is the value for $N1$, and also the value for $N2$.

The Sample Size Per Group must be ≥ 2 . You can enter a single value or a series of values.

$N1$ (Sample Size, Group 1)

*This option is displayed if Group Allocation = "Enter $N1$ and $N2$ individually" or "Enter $N1$ and R , where $N2 = R * N1$."*

$N1$ is the number of items or individuals sampled from the Group 1 population.

$N1$ must be ≥ 2 . You can enter a single value or a series of values.

Equivalence Tests for the Ratio of Two Negative Binomial Rates

N2 (Sample Size, Group 2)

This option is displayed only if Group Allocation = "Enter N1 and N2 individually."

$N2$ is the number of items or individuals sampled from the Group 2 population.

$N2$ must be ≥ 2 . You can enter a single value or a series of values.

R (Group Sample Size Ratio)

*This option is displayed only if Group Allocation = "Enter N1 and R, where $N2 = R * N1$."*

R is the ratio of $N2$ to $N1$. That is,

$$R = N2/N1$$

Use this value to obtain $N2$ as a multiple (or proportion) of $N1$.

$N2$ is calculated from $N1$ using the formula:

$$N2 = [R \times N1],$$

where the value $[Y]$ is the next integer $\geq Y$.

For example, setting $R = 2.0$ results in a Group 2 sample size that is double the sample size in Group 1.

R must be greater than 0. If $R < 1$, then $N2$ will be less than $N1$; if $R > 1$, then $N2$ will be greater than $N1$. You can enter a single value or a series of values.

Total Sample Size (N)

This option is displayed only if Group Allocation = "Enter total sample size and percentage in Group 1."

This is the total sample size, or the sum of the two group sample sizes. This value, along with the percentage of the total sample size in Group 1, implicitly defines $N1$ and $N2$.

The total sample size must be greater than one, but practically, must be greater than 3, since each group sample size needs to be at least 2.

You can enter a single value or a series of values.

Percent in Group 1

This option is displayed only if Group Allocation = "Enter total sample size and percentage in Group 1."

This value fixes the percentage of the total sample size allocated to Group 1. Small variations from the specified percentage may occur due to the discrete nature of sample sizes.

The Percent in Group 1 must be greater than 0 and less than 100. You can enter a single value or a series of values.

Effect Size

RU (Upper Equivalence Limit)

Enter the upper equivalence limit for the ratio of the two Negative Binomial event rates (λ_2 / λ_1). This value is entered as a ratio, not a percentage. When the ratio of the Negative Binomial event rates is between this value and RL , the two rates are said to be 'equivalent'. This value must be greater than one. Common choices are 1.1, 1.2, 1.25, and $1/RL$. If you enter ' $1/RL$ ', RU will be calculated from RL as $RU = 1/RL$. The choice ' $1/RL$ ' is popular because RL and $RU = 1/RL$ are limits that are of equal magnitude on the log scale.

Equivalence Tests for the Ratio of Two Negative Binomial Rates

RL (Lower Equivalence Limit)

Enter the lower equivalence limit for the ratio of the two Negative Binomial event rates (λ_2 / λ_1). This value is entered as a ratio, not a percentage. When the ratio of the Negative Binomial event rates is between this value and RU, the two rates are said to be 'equivalent'. This value must be less than one. Common choices are 0.8, 0.9, and $1/RU$. If you enter ' $1/RU$ ', RL will be calculated from RU as $RL = 1/RU$. The choice ' $1/RU$ ' is popular because RU and $RL = 1/RU$ are limits that are of equal magnitude on the log scale.

λ_1 (Event Rate of Group 1)

Enter a value (or range of values) for the mean event rate per time unit in group 1 (control).

Example of Estimating λ_1

If 200 patients were exposed for 1 year (i.e. $t_1 = 1$ year) and 40 experienced the event of interest, then the mean event rate would be $\lambda_1 = 40/(200*1) = 0.2$ per patient-year. If 200 patients were exposed for 2 years (i.e. $t_1 = 2$ years) and 40 experienced the event of interest, then the mean event rate would be $\lambda_1 = 40/(200*2) = 0.1$ per patient-year.

λ_1 is used with λ_2 to calculate the event rate ratio as λ_2 / λ_1 . The range is $\lambda_1 > 0$. You can enter a single value such as 1 or a series of values such as 1 1.2 1.4 or 1 to 2 by 0.5.

Enter λ_2 or Ratio for Group 2

Indicate whether to enter the Group 2 event rate (λ_2) directly or the event rate ratio (λ_2 / λ_1) to specify λ_2 . The event rate ratio is calculated from λ_2 and λ_1 as λ_2 / λ_1 .

λ_2 (Event Rate of Group 2)

Enter a value (or range of values) for the mean event rate per time unit in group 2 (treatment).

Example of Estimating λ_2

If 200 patients were exposed for 1 year (i.e. $t_1 = 1$ year) and 40 experienced the event of interest, then the mean event rate would be $\lambda_2 = 40/(200*1) = 0.2$ per patient-year. If 200 patients were exposed for 2 years (i.e. $t_1 = 2$ years) and 40 experienced the event of interest, then the mean event rate would be $\lambda_2 = 40/(200*2) = 0.1$ per patient-year.

λ_1 is used with λ_2 to calculate the event rate ratio as λ_2 / λ_1 . The range is $\lambda_2 > 0$. You can enter a single value such as 1 or a series of values such as 1 1.2 1.4 or 1 to 2 by 0.5.

λ_2 / λ_1 (Ratio of Event Rates)

This is the (assumed, known, true) value of the ratio of the two event rates, λ_1 and λ_2 , at which the power is to be calculated. The event rate ratio is calculated from λ_1 and λ_2 as λ_2 / λ_1 . The range is $\lambda_2 / \lambda_1 > 0$ and $RL < \lambda_2 / \lambda_1 < RU$. You can enter a single value such as 1 or a series of values such as 0.9 0.95 1 1.05 1.1 or 0.9 to 1.1 by 0.05.

ϕ (Dispersion)

Enter a value or series of values for the anticipated Negative Binomial dispersion. You can enter a single value such as 0.4 or a series of values such as 0.2 0.3 0.4 0.5 or 0.2 to 0.5 by 0.1.

Equivalence Tests for the Ratio of Two Negative Binomial Rates

Example 1 – Calculating Sample Size

Researchers wish to determine whether the average Negative Binomial rate of those receiving a new treatment is equivalent to a current control. The average exposure time for all subjects is 1.6 years. The two treatments will be considered equivalent if the event rate ratio is between 0.8 and 1.25. The event rate of the control group is 2.2 events per year. The researchers would like to examine the effect on sample size of a range of treatment group event rates from 1.9 to 2.5. Dispersion values ranging from 0.2 to 0.5 will be considered.

The desired power is 0.9 and the significance level will be 0.025. The variance calculation method used will be the method where the assumed rates are used.

Setup

This section presents the values of each of the parameters needed to run this example. First load the **Equivalence Tests for the Ratio of Two Negative Binomial Rates** procedure window from the menus. You may then make the appropriate entries as listed below, or open **Example 1** by going to the **File** menu and choosing **Open Example Template**.

Option	Value
Design Tab	
Solve For	Sample Size
Variance Calculation Method.....	Using Assumed True Rates
Power.....	0.90
Alpha.....	0.025
$\mu(t)$ (Average Exposure Time)	1.6
Group Allocation	Equal (N1 = N2)
RU (Upper Equivalence Limit)	1.25
RL (Lower Equivalence Limit).....	0.8
λ_1 (Event Rate of Group 1).....	2.2
Enter λ_2 or Ratio for Group 2	λ_2 (Event Rate of Group 2)
λ_2 (Event Rate of Group 2).....	1.9 to 2.5 by 0.1
ϕ (Dispersion)	0.2 to 0.5 by 0.05

Equivalence Tests for the Ratio of Two Negative Binomial Rates

Annotated Output

Click the Calculate button to perform the calculations and generate the following output.

Numeric Results

Numeric Results for Equivalence Tests of the Ratio of Two Negative Binomial Rates

H0: $\lambda_2 / \lambda_1 \leq RL$ or $\lambda_2 / \lambda_1 \geq RU$ vs.

H1: $RL < \lambda_2 / \lambda_1 < RU$

Variance Calculation Method: Using Assumed True Rates

Power	N1	N2	N	Average Exposure Time $\mu(t)$	Grp 1 Cntrl Event Rate λ_1	Grp 2 Trt Event Rate λ_2	Event Rate Ratio λ_2 / λ_1	Lower Equiv. Limit RL	Upper Equiv. Limit RU	Dispersion ϕ	Alpha
0.90001	1817	1817	3634	1.60	2.20	1.90	0.864	0.800	1.250	0.20	0.025
0.90009	641	641	1282	1.60	2.20	2.00	0.909	0.800	1.250	0.20	0.025
0.90067	333	333	666	1.60	2.20	2.10	0.955	0.800	1.250	0.20	0.025
0.90048	253	253	506	1.60	2.20	2.20	1.000	0.800	1.250	0.20	0.025
0.90042	317	317	634	1.60	2.20	2.30	1.045	0.800	1.250	0.20	0.025
0.90025	536	536	1072	1.60	2.20	2.40	1.091	0.800	1.250	0.20	0.025
0.90014	1081	1081	2162	1.60	2.20	2.50	1.136	0.800	1.250	0.20	0.025
0.90010	1997	1997	3994	1.60	2.20	1.90	0.864	0.800	1.250	0.25	0.025
0.90036	706	706	1412	1.60	2.20	2.00	0.909	0.800	1.250	0.25	0.025
0.90074	367	367	734	1.60	2.20	2.10	0.955	0.800	1.250	0.25	0.025
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References

Zhu, H. 2016. 'Sample Size Calculation for Comparing Two Poisson or Negative Binomial Rates in Non-Inferiority or Equivalence Trials.' Statistics in Biopharmaceutical Research, Accepted Manuscript.

Report Definitions

Power is the probability of rejecting the null hypothesis when it is false.

N1 and N2 are the number of subjects in groups 1 and 2, respectively.

N is the total sample size. $N = N1 + N2$.

$\mu(t)$ is the average exposure (observation) time across subjects in both groups.

λ_1 is the event rate per time unit in Group 1 (control).

λ_2 is the event rate per time unit in Group 2 (treatment).

λ_2 / λ_1 is the (known, true, assumed) ratio of the two event rates.

RL and RU are the respective lower and upper equivalence limits for the event rate ratio.

Dispersion (ϕ) is the Negative Binomial dispersion parameter.

Alpha is the probability of rejecting the null hypothesis when it is true.

Summary Statements

For an equivalence test of H0: $\lambda_2 / \lambda_1 \leq 0.800$ or $\lambda_2 / \lambda_1 \geq 1.250$ vs. H1: $0.800 < \lambda_2 / \lambda_1 < 1.250$, and using the variance calculation method with assumed true rates, samples of 1817 and 1817 subjects with average exposure time 1.60 achieve 90.001% power to detect an event rate ratio λ_2 / λ_1 of 0.864 when the event rate in group 1 (λ_1) is 2.20, the event rate in group 2 (λ_2) is 1.90, the Negative Binomial dispersion is 0.20, and the significance level (alpha) is 0.025.

Equivalence Tests for the Ratio of Two Negative Binomial Rates

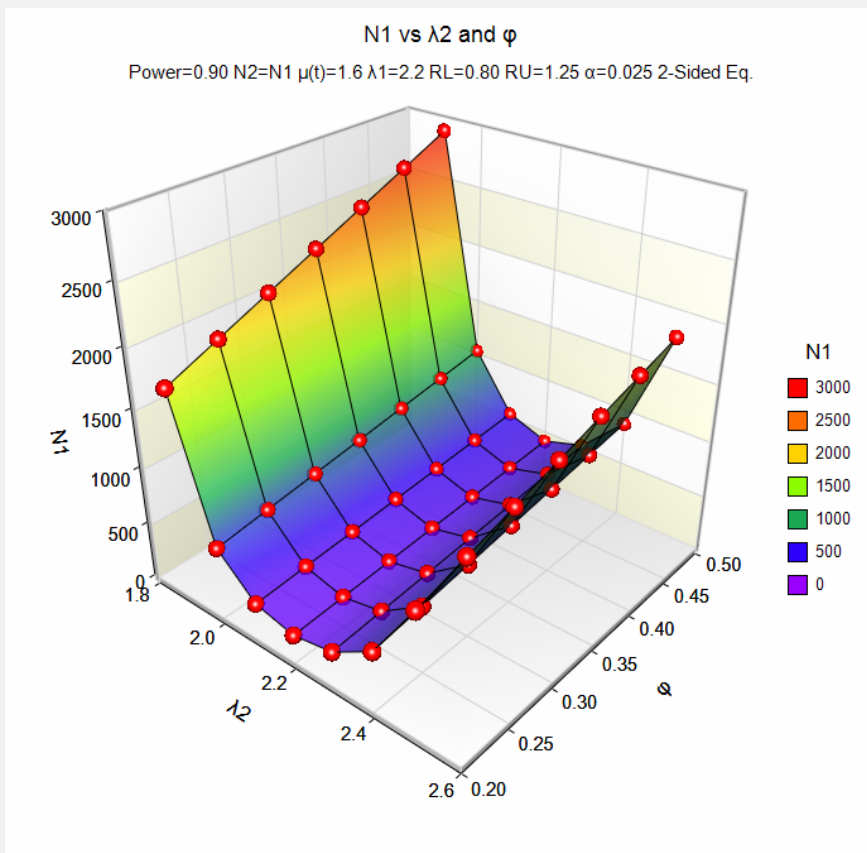
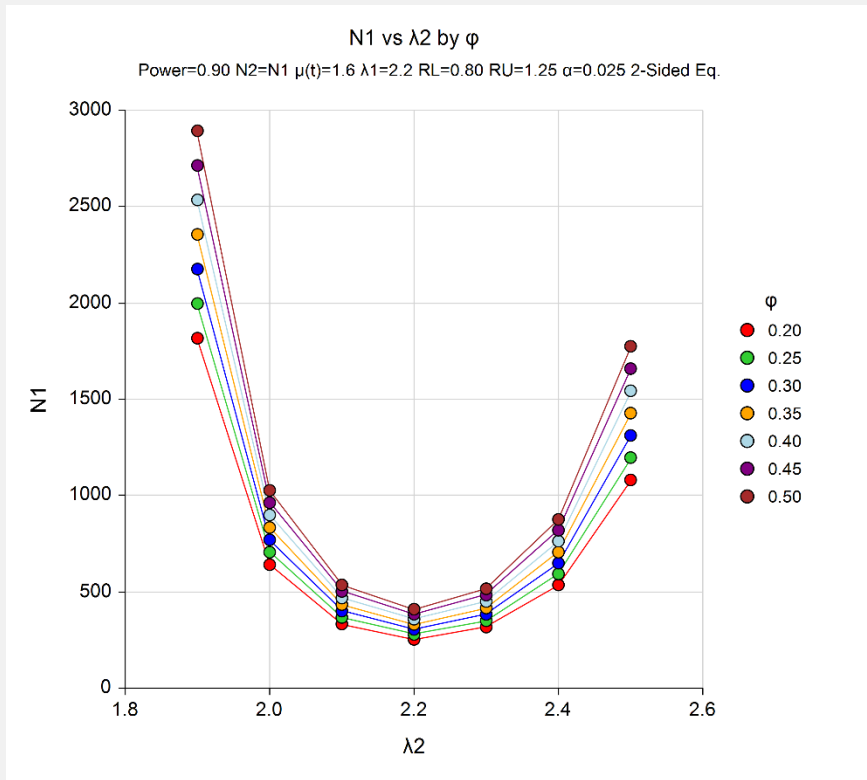
Dropout Rate	Dropout-Inflated Sample Size			Dropout-Inflated Enrollment Sample Size			Expected Number of Dropouts		
	N1	N2	N	N1'	N2'	N'	D1	D2	D
20%	1817	1817	3634	2272	2272	4544	455	455	910
20%	641	641	1282	802	802	1604	161	161	322
20%	333	333	666	417	417	834	84	84	168
20%	253	253	506	317	317	634	64	64	128
20%	317	317	634	397	397	794	80	80	160
20%	536	536	1072	670	670	1340	134	134	268
20%	1081	1081	2162	1352	1352	2704	271	271	542
20%	1997	1997	3994	2497	2497	4994	500	500	1000
20%	706	706	1412	883	883	1766	177	177	354
20%	367	367	734	459	459	918	92	92	184
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Definitions
 Dropout Rate (DR) is the percentage of subjects (or items) that are expected to be lost at random during the course of the study and for whom no response data will be collected (i.e. will be treated as "missing").
 N1, N2, and N are the evaluable sample sizes at which power is computed. If N1 and N2 subjects are evaluated out of the N1' and N2' subjects that are enrolled in the study, the design will achieve the stated power.
 N1', N2', and N' are the number of subjects that should be enrolled in the study in order to end up with N1, N2, and N evaluable subjects, based on the assumed dropout rate. After solving for N1 and N2, N1' and N2' are calculated by inflating N1 and N2 using the formulas $N1' = N1 / (1 - DR)$ and $N2' = N2 / (1 - DR)$, with N1' and N2' always rounded up. (See Julious, S.A. (2010) pages 52-53, or Chow, S.C., Shao, J., and Wang, H. (2008) pages 39-40.)
 D1, D2, and D are the expected number of dropouts. $D1 = N1' - N1$, $D2 = N2' - N2$, and $D = D1 + D2$.

This report shows the sample sizes for the indicated scenarios.

Equivalence Tests for the Ratio of Two Negative Binomial Rates

Plots Section



These plots represent the required sample sizes for various values of λ_2 and the dispersion parameter.

Equivalence Tests for the Ratio of Two Negative Binomial Rates

Example 2 – Validation using Zhu (2016)

Zhu (2016) presents an example of solving for sample size where the event rates are both 2.5, the dispersion parameter is 0.35, the average duration is 0.9, the equivalence limits are 0.875 and 1.14 ($1 / 0.875$), the power is 0.9, and the Type I error rate is 0.05.

The calculated total sample sizes are 965, 966, and 966 for the Assumed True Rate, and Fixed Marginal Total, and REML variance calculation methods, respectively.

Setup

This section presents the values of each of the parameters needed to run this example. First load the **Equivalence Tests for the Ratio of Two Negative Binomial Rates** procedure window from the menus. You may then make the appropriate entries as listed below, or open **Example 2 (a, b, or c)** by going to the **File** menu and choosing **Open Example Template**.

<u>Option</u>	<u>Value</u>
Design Tab	
Solve For	Sample Size
Variance Calculation Method.....	Using Assumed True Rates (2nd run: Fixed Marginal Total 3rd run: Restricted Maximum Likelihood Estimation)
Power.....	0.90
Alpha.....	0.05
$\mu(t)$ (Average Exposure Time).....	0.9
Group Allocation	Equal (N1 = N2)
RU (Upper Equivalence Limit)	1/RL
RL (Lower Equivalence Limit).....	0.875
λ_1 (Event Rate of Group 1).....	2.5
Enter λ_2 or Ratio for Group 2	λ_2 / λ_1 (Ratio of Event Rates)
λ_2 / λ_1 (Ratio of Event Rates).....	1
ϕ (Dispersion)	0.35

Output

Click the Calculate button to perform the calculations and generate the following output.

Numeric Results

Numeric Results for Equivalence Tests of the Ratio of Two Negative Binomial Rates											
H0: $\lambda_2 / \lambda_1 \leq RL$ or $\lambda_2 / \lambda_1 \geq RU$ vs.											
H1: $RL < \lambda_2 / \lambda_1 < RU$											
Variance Calculation Method: Using Assumed True Rates											
Power	N1	N2	N	Average Exposure Time $\mu(t)$	Grp 1 Cntrl Event Rate λ_1	Grp 2 Trt Event Rate λ_2	Event Rate Ratio λ_2 / λ_1	Lower Equiv. Limit RL	Upper Equiv. Limit RU	Disper- sion ϕ	Alpha
0.90022	965	965	1930	0.90	2.50	2.50	1.000	0.875	1.250	0.35	0.050
Variance Calculation Method: Fixed Marginal Total or REML											
0.90015	966	966	1932	0.90	2.50	2.50	1.000	0.875	1.250	0.35	0.050
Variance Calculation Method: Restricted Maximum Likelihood Estimation											
0.90034	966	966	1932	0.90	2.50	2.50	1.000	0.875	1.250	0.35	0.050

The sample sizes calculated in **PASS** match those of Zhu (2016) exactly.